

1.1.1

$$[S] = \frac{1}{2} \begin{bmatrix} 0 & -j\sqrt{2} & -j\sqrt{2} \\ -j\sqrt{2} & -1 & 1 \\ -j\sqrt{2} & 1 & -1 \end{bmatrix}$$

1.1.2

$$[S] = \frac{1}{2} \begin{bmatrix} 0 & -j\sqrt{2} & -j\sqrt{2} \\ -j\sqrt{2} & 1 & -1 \\ -j\sqrt{2} & -1 & 1 \end{bmatrix}$$

1.2.1

$$[S] = \begin{bmatrix} 0 & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{4} & \frac{1}{4} \\ \frac{1}{2} & \frac{1}{4} & \frac{1}{4} \end{bmatrix}$$

1.2.2

$$[S] = \begin{bmatrix} 0 & \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & 0 & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} & 0 \end{bmatrix}$$

1.3.1

$$[S] = \frac{-j}{\sqrt{2}} \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

1.4.1

$$[S] = \frac{1}{\sqrt{2}} \begin{bmatrix} 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & -1 \\ 1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \end{bmatrix}$$

1.4.2

$$[S] = \frac{1}{\sqrt{2}} \begin{bmatrix} 0 & 0 & 1-j & 1-j \\ 0 & 0 & -1 & 1 \\ 1-j & 1 & 0 & 0 \\ -j & 1 & 0 & 0 \end{bmatrix}$$

2.2

$$S_{11} = 0.9 \angle -55^\circ = 0.516 - 0.737j$$

$$S_{12} = 0.03 \angle -60^\circ = 0.015 - 0.026j$$

$$S_{21} = 3 \angle 125^\circ = -1.72 + 2.457j$$

$$S_{22} = 0.7 \angle -30^\circ = 0.606 - 0.35j$$

$$|A| = |S_{11} S_{22} - S_{21} S_{12}| = |0.055 - 0.627j - (0.038 + 0.082j)| =$$

$$= |0.017 - 0.709j| = \begin{cases} r = 0.709 \\ \theta = -88.65^\circ \end{cases}$$

$$|A| = 0.709 < 1 \quad \text{OK}$$

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |A|^2}{2 |S_{21} \cdot S_{12}|} = \frac{1 - 0.9^2 - 0.7^2 + 0.709^2}{2 |0.038 + 0.082j|} =$$

$$= \frac{1 - 0.81 - 0.49 + 0.502}{2 \cdot 9.04 \cdot 10^{-2}} = 1.117$$

$$K = 1.117 > 1 \quad \text{OK}$$

INCONDICIONALMENTE
ESTABLE //

$$|A| < 1$$

$$K > 1$$

2.3

$$S_{11} = 0.75 \angle 180^\circ = -0.75$$

$$S_{12} = 0.04 \angle 45^\circ = 0.028 + 0.028j$$

$$S_{21} = 3 \angle 75^\circ = 0.776 + 2.898j$$

$$S_{22} = 0.4 \angle -40^\circ = 0.306 - 0.257j$$

$$\begin{aligned} |A| &= |S_{11} S_{22} - S_{21} S_{12}| = |-0.2295 + 0.193j - (-0.059 + 0.103j)| = \\ &= |-0.17 + 0.09j| = \begin{cases} r = 0.192 \\ \theta = 152.1^\circ \end{cases} \end{aligned}$$

$$|A| = 0.192 < 1 \quad \text{OK}$$

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |A|^2}{2 \cdot |S_{21} S_{12}|} = \frac{1 - 0.75^2 - 0.4^2 + 0.192^2}{2 \cdot |-0.059 - 0.103j|} =$$

$$= \frac{1 - 0.5625 - 0.16 + 0.0369}{2 \cdot 0.119} = 1.32$$

$$K = 1.32 > 1 \quad \text{OK}$$

INCONDICIONALMENTE
ESTABLE

$$|A| < 1$$

$$K > 1$$

2.1

$$S_{11} = 0.6 \angle -90^\circ = 0 - 0.6j$$

$$S_{12} = 0.06 \angle -50^\circ = 0.039 - 0.046j$$

$$S_{21} = 2.5 \angle 75^\circ = 0.647 + 2.415j$$

$$S_{22} = 0.6 \angle -60^\circ = 0.3 - 0.52j$$

$$\begin{aligned} |A| &= |S_{11} S_{22} - S_{21} S_{12}| = |-0.312 - 0.78j - (0.136 + 0.064j)| \\ &= |-0.448 - 0.244j| \end{aligned} \left. \begin{array}{l} r = 0.51 \\ \theta = -151.4^\circ \end{array} \right\}$$

$$|A| = 0.51 < 1 \quad \text{OK}$$

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |A|^2}{2 |S_{21} S_{12}|} = \frac{1 - 0.6^2 - 0.6^2 + 0.51^2}{2 |0.136 + 0.064j|} =$$

$$= \frac{1 - 0.36 - 0.36 + 0.2601}{2 \cdot 0.15} = 1.8$$

$$K = 1.8 > 1 \quad \text{OK}$$

INCONDICIONALMENTE
ESTABLE

$$|A| < 1$$

$$\vee \\ K > 1$$